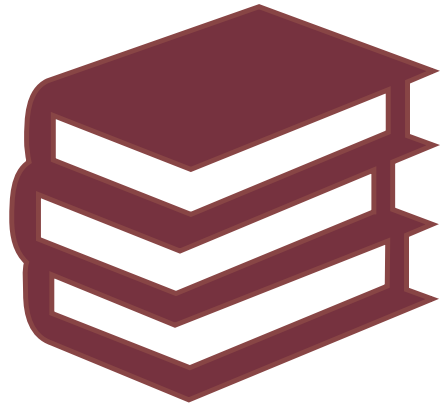


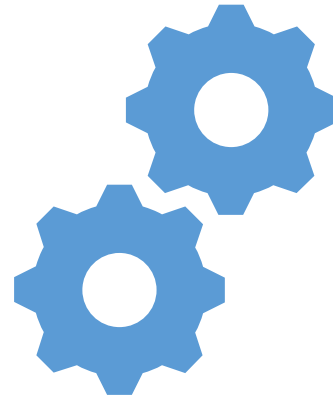
Design And Optimization Of Aeronautical Components And Digital Twins Development

A. Lopez, U. Cella, C. Groth, M. E. Biancolini

Università di Roma, Tor Vergata



Introduction



Design And Optimization



Results

Introduction: Case Study



First task:

- Design and optimization of scoop air intake

Second task:

- Digital twin development of scoop air intake

Objective:

- The aim is to create an accurate and reliable model that allows to evaluate in real time both scalar quantities and field quantities;
- The generated model can be integrated with the rest of the aircraft;



Mesh Morphing RBF (Radial Basis Function)

$$\begin{aligned}
 f^x(x) &= \sum_{i=1}^m \gamma_i^x \phi(\|c_i - x\|) + \beta_1^x + \beta_2^x x_1 + \beta_3^x x_2 + \beta_4^x x_3 \\
 f^y(x) &= \sum_{i=1}^m \gamma_i^y \phi(\|c_i - x\|) + \beta_1^y + \beta_2^y x_1 + \beta_3^y x_2 + \beta_4^y x_3 \\
 f^z(x) &= \sum_{i=1}^m \gamma_i^z \phi(\|c_i - x\|) + \beta_1^z + \beta_2^z x_1 + \beta_3^z x_2 + \beta_4^z x_3
 \end{aligned}$$

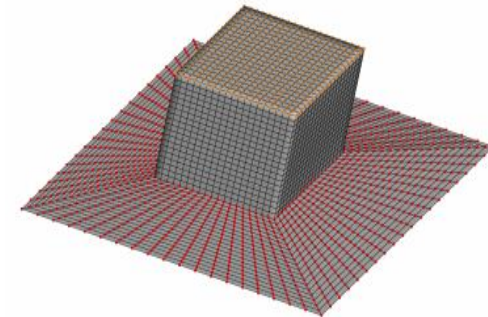
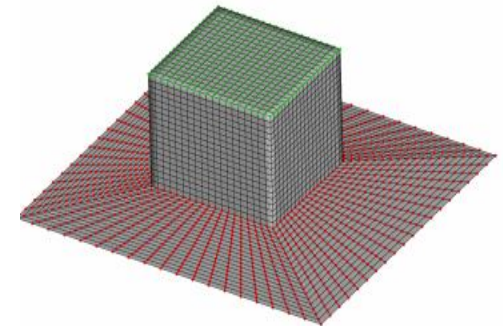
Weight and radial function

Polynomial term

$$\begin{bmatrix} M & P \\ P^T & 0 \end{bmatrix} \begin{Bmatrix} \gamma \\ \beta \end{Bmatrix} = \begin{Bmatrix} g \\ 0 \end{Bmatrix}$$

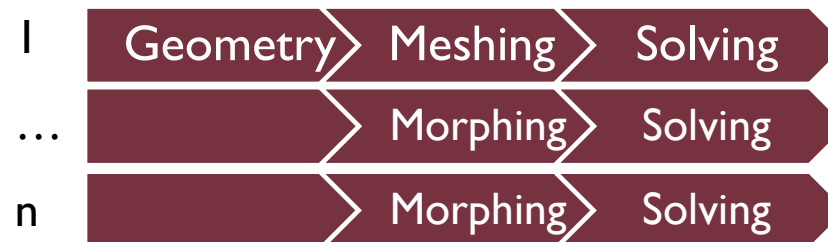
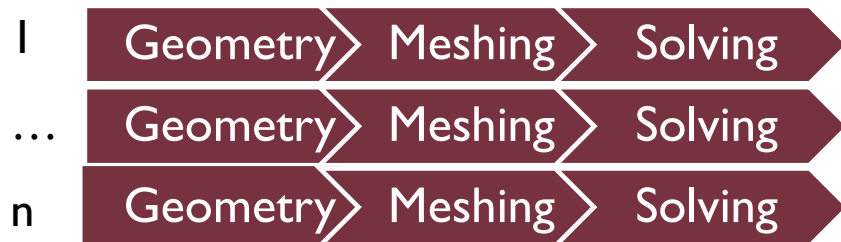
With $M = \phi(\|c_i - c_j\|)$
 $P_j = [1 \ x_1 \ x_2 \ \dots \ x_n]$

Boundary conditions



Classic

RBF



Optimization workflow Response surface



- Linear Regression:

$$y_i = \beta_0 + \beta_1 X_{i1} + \beta_2 X_{i2} + \beta_3 X_{i3} + \varepsilon_i$$

$$y_i = \beta_0 + \beta_1 X_{i1} + \beta_2 X_{i2} + \beta_3 X_{i1}^3 + \beta_4 X_{i2}^2 + \varepsilon_i$$

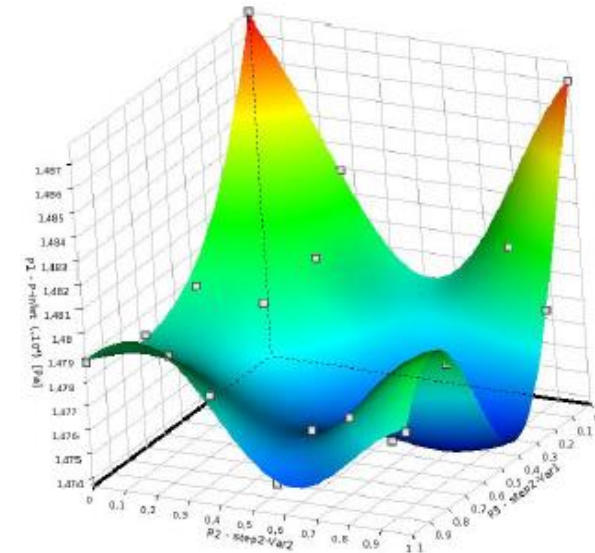
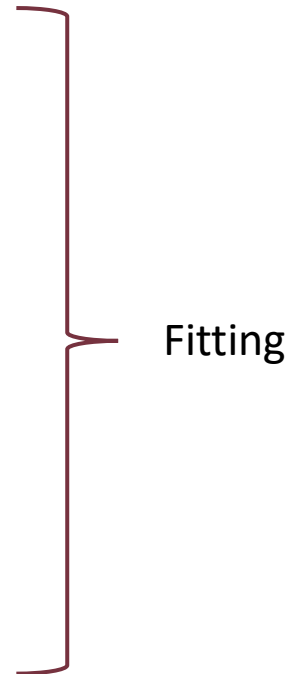
$$y_i = \beta_0 + \beta_1 X_{i1} + \beta_2 X_{i2} + \beta_3 X_{i1} X_{i2} + \beta_4 \log X_{i3} + \varepsilon_i$$

- A weighted linear combination of RBF functions

$$f(x) = \sum_1^n \omega_i \phi(\|x - c_i\|)$$

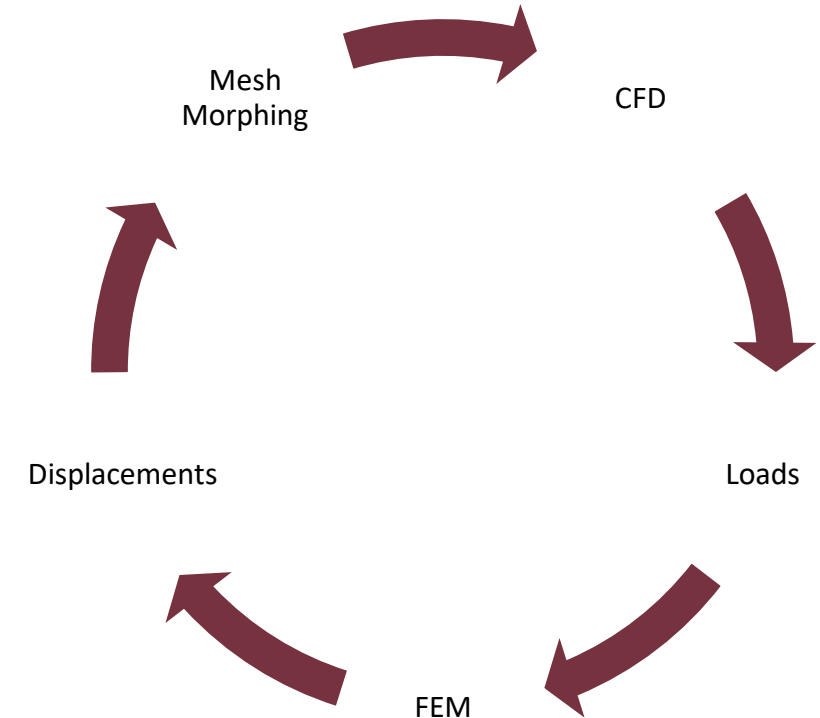
- Neural network

- ...



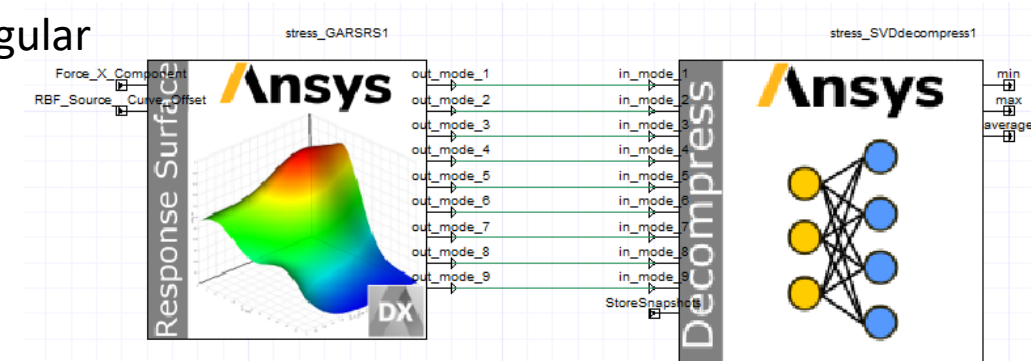
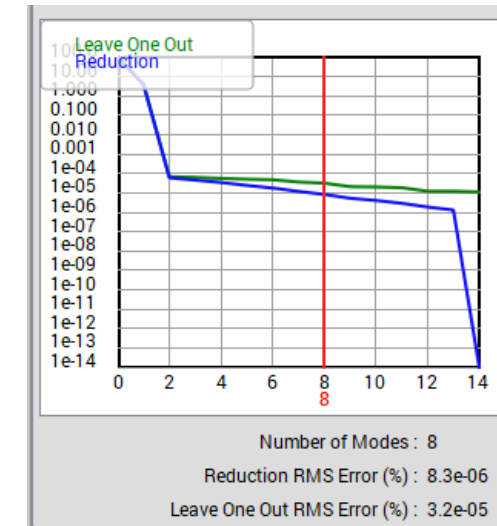
Fluid-Structure-Interaction (FSI)

- To study fluid-structure interaction with high-fidelity analysis there are generally two approaches:
 - 1 way
 - 2 ways
 - Modal Superposition
- In this study, the focus is on the two-way method:
 - From the CFD analysis, the aerodynamic loads are calculated and exported;
 - The loads are imported into the FEM model and the displacements are estimated;
 - The displacements are used to deform the CFD mesh and have a more accurate estimate of the loads.
 - The workflow is iterated until forces and displacements converge



Digital twin development: SVD + ROM

- One of the best-known applications of SVD is Principal Component Analysis (PCA);
- Given a matrix $A \in \mathbb{R}^m \times n$ and given $p = \min(m, n)$, a singular value decomposition (SVD) of A is a factorization of the form:
$$A = U \Sigma^t V$$
- $U = (u_1 \dots u_m) \in \mathbb{R}^m \times m$ and $V = (v_1 \dots v_n) \in \mathbb{R}^n \times n$ are orthogonal and $\Sigma \in \mathbb{R}^m \times n$ is (pseudo)diagonal with diagonal elements $\sigma_1 \geq \dots \geq \sigma_p \geq 0$
- $\sigma_1, \dots, \sigma_p$ are the singular values of A
- A can be rewritten as: $A = \sum_1^k \alpha_i U_i$, where k are the principal singular values
- Finally, to construct the ROM it is necessary to find a correlation between input parameters and mode weights, and several interpolation methods can be used (RBF, Polynomial/Gaussian Regression, neural networks)



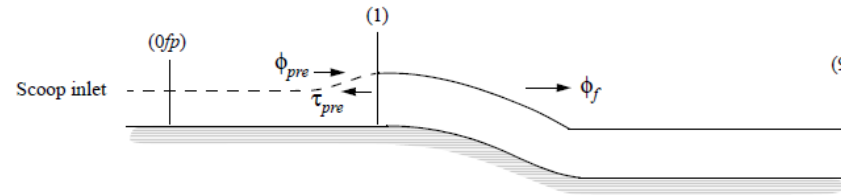
Design baseline: ESDU 86002

Input:

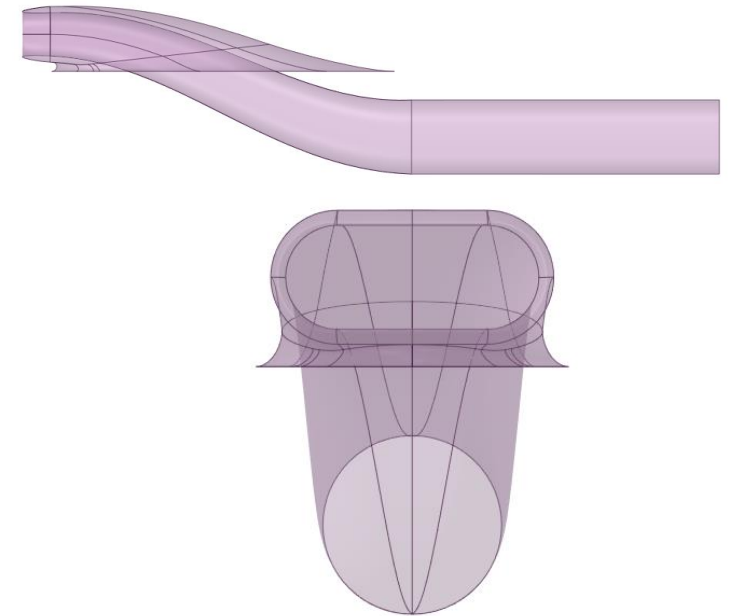
- Required massflow
- Momentum thickness
- Boundary layer thickness
- Mach number

Output:

- Sizing



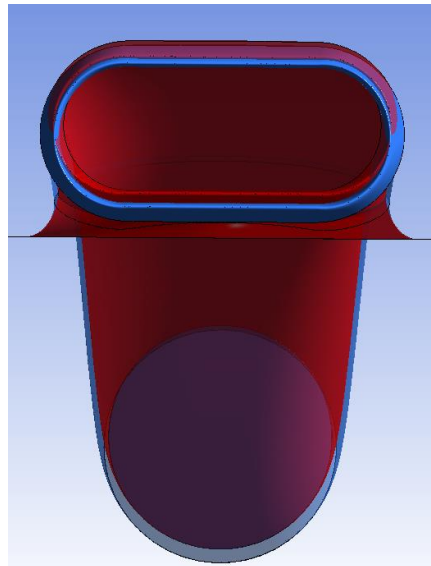
Some images extracted from the standard



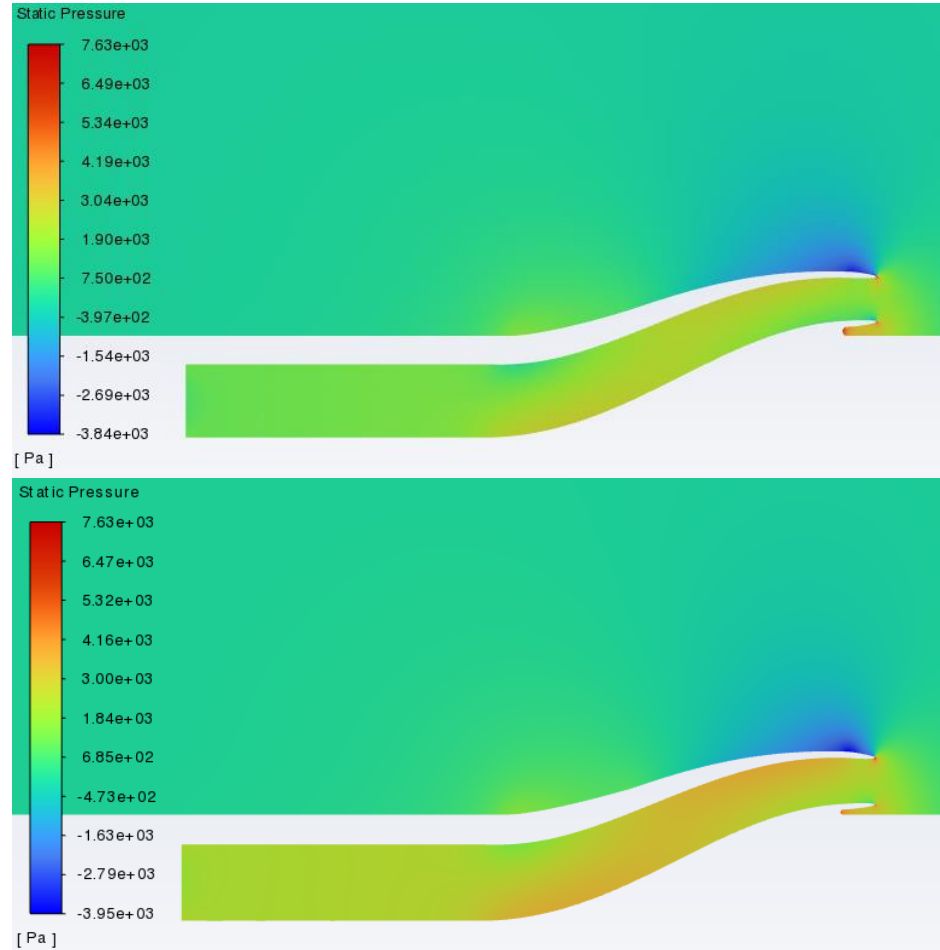
CAD baseline

CFD Optimization

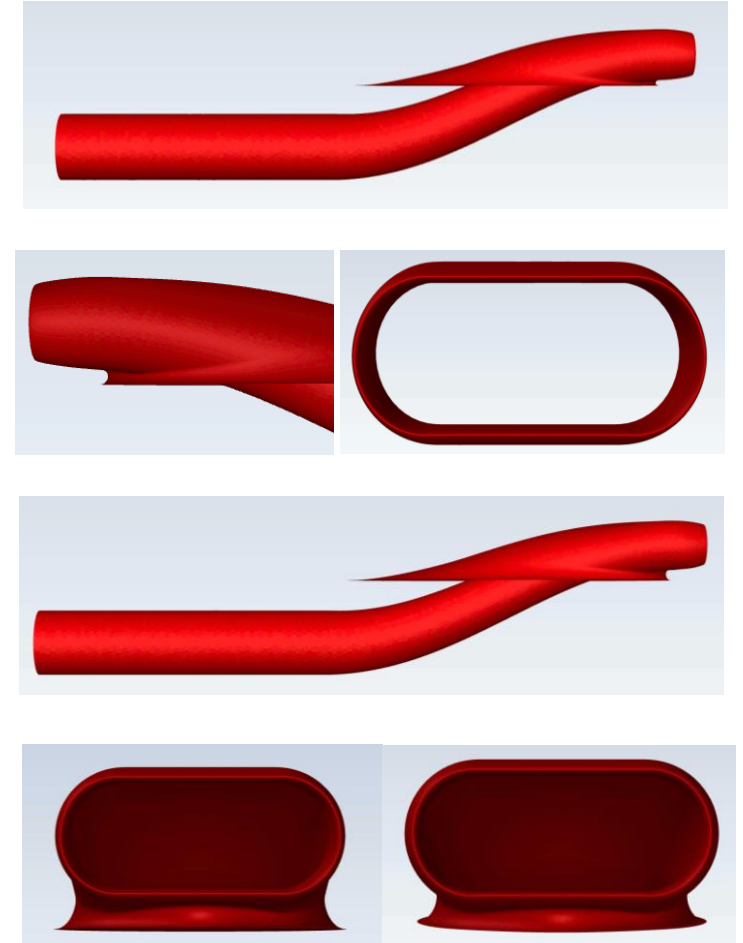
- Drag -32%
- Outlet pressure +86%



Comparison of baseline (red) and optimized (blue)



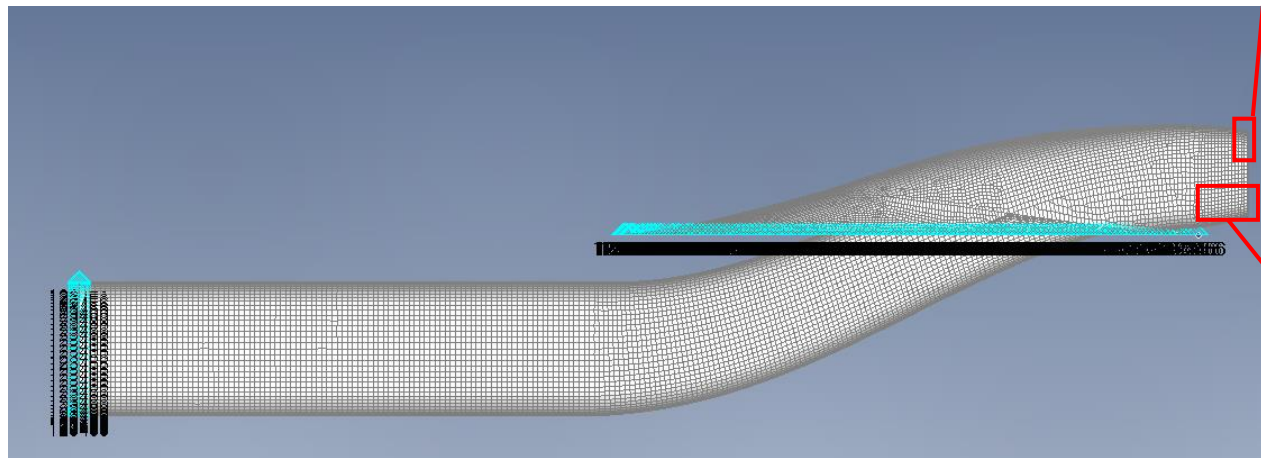
Pressure on symmetric plane baseline (above) and optimized (below)



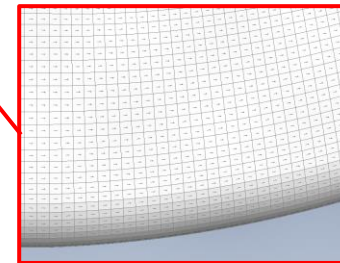
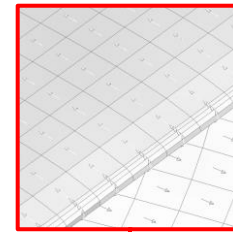
6 shape parameters

FEM Analysis: Mesh and parameters

- Laminate Plate, Linear elements: 48874
- Tsai-Wu Failure Theory
- Constraints: Fixed curves
- Loads: Pressure field of the most critical point (FSI)
- Parameters: Number and angle of plies



Morphed mesh



Material orientation

| | |
|------------------------------------|-----------|
| Density [kg/m^3] | 1530 |
| E11 [Pa] | 1.83 E+11 |
| E22 [Pa] | 9 E+9 |
| G12 [Pa] | 8 E+9 |
| G1z [Pa] | 8 E+9 |
| G2z [Pa] | 4 E+9 |
| X1t [Pa] | 1.5 E+9 |
| X2t [Pa] | 9.5 E+8 |
| X1c [Pa] | 7 E+7 |
| X2c [Pa] | 2 E+8 |
| S12 [Pa] | 8 E+7 |
| nu | 0.35 |

Material property

FEM Analysis: Number of plies

Baseline:

- 24 Plies of 0.25 mm
- Lamination sequence: [45/-45/02/90/02/45/-45/02]s

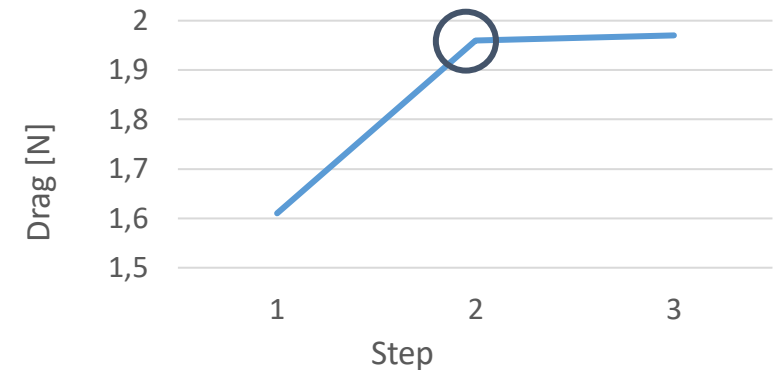
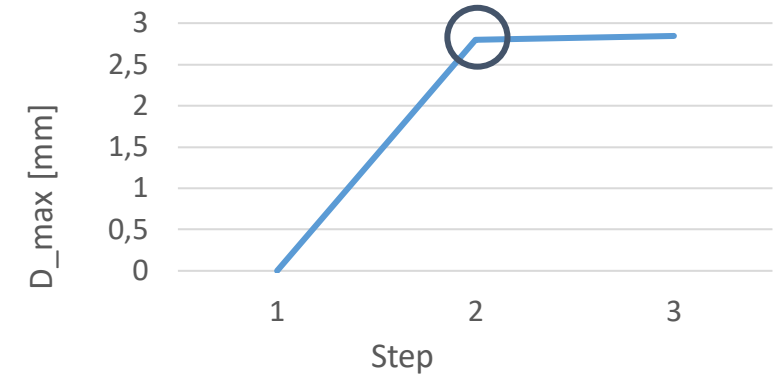
Optimized number of plies:

- 4 Plies of 0.125 mm
- Lamination sequence: [0/90]s

Mass reduction: -92%

| | Delta |
|-------|--------|
| Drag | +0.3 N |
| P_Out | +0.3% |

Variation of CFD performances



Convergence of FSI workflow

FEM ROM: Commercial software

Input:

- 2 angle value

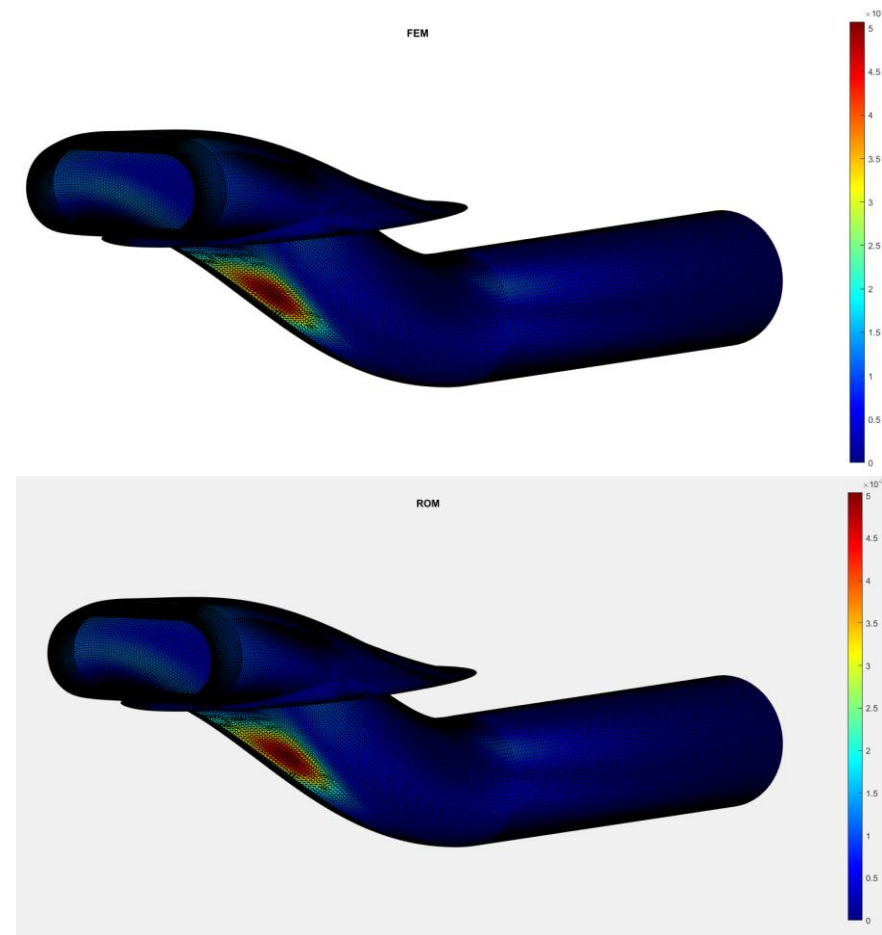
Output:

- Displacements field

Ansys Twin Builder was used to identify the relationship between input parameters and mode weights

ROM Relative error < 5%

Exported as .fmu



Comparison of FEM (left) and ROM (right) displacements for a random point of the test set

FEM ROM:
Matlab code

Input:

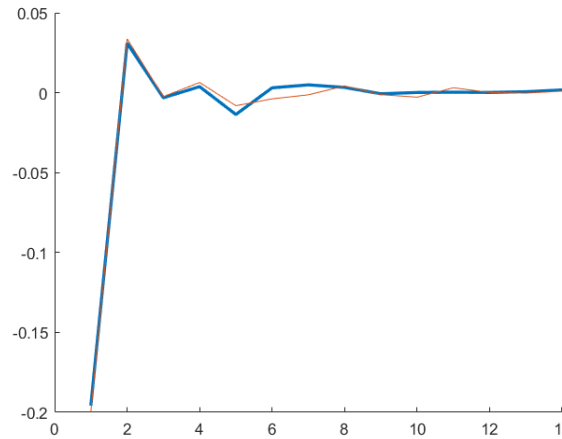
- 2 angle value

Output:

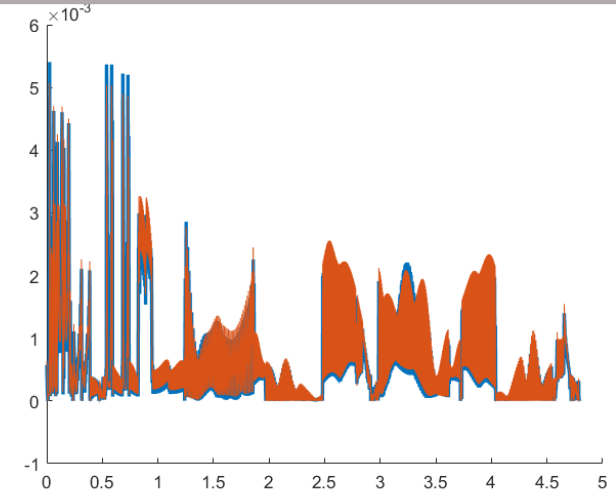
- Displacements field

A neural network was trained to identify the relationship between input parameters and mode weights

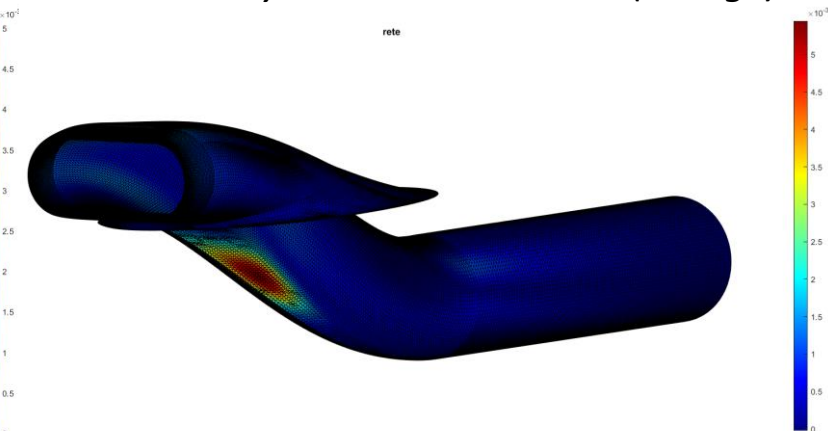
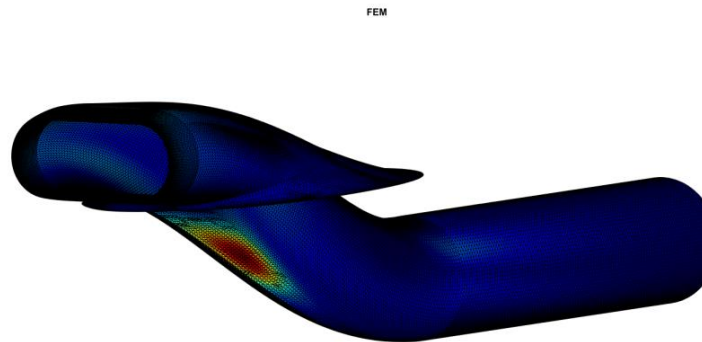
ROM Relative error < 6%



Weight of modes real (blue) and calculated by the neural network (orange)



Displacement value for each node real (blue) and calculated by the neural network (orange)



Comparison of FEM (left) and ROM (right) displacements for a random point of the test set

CFD ROM

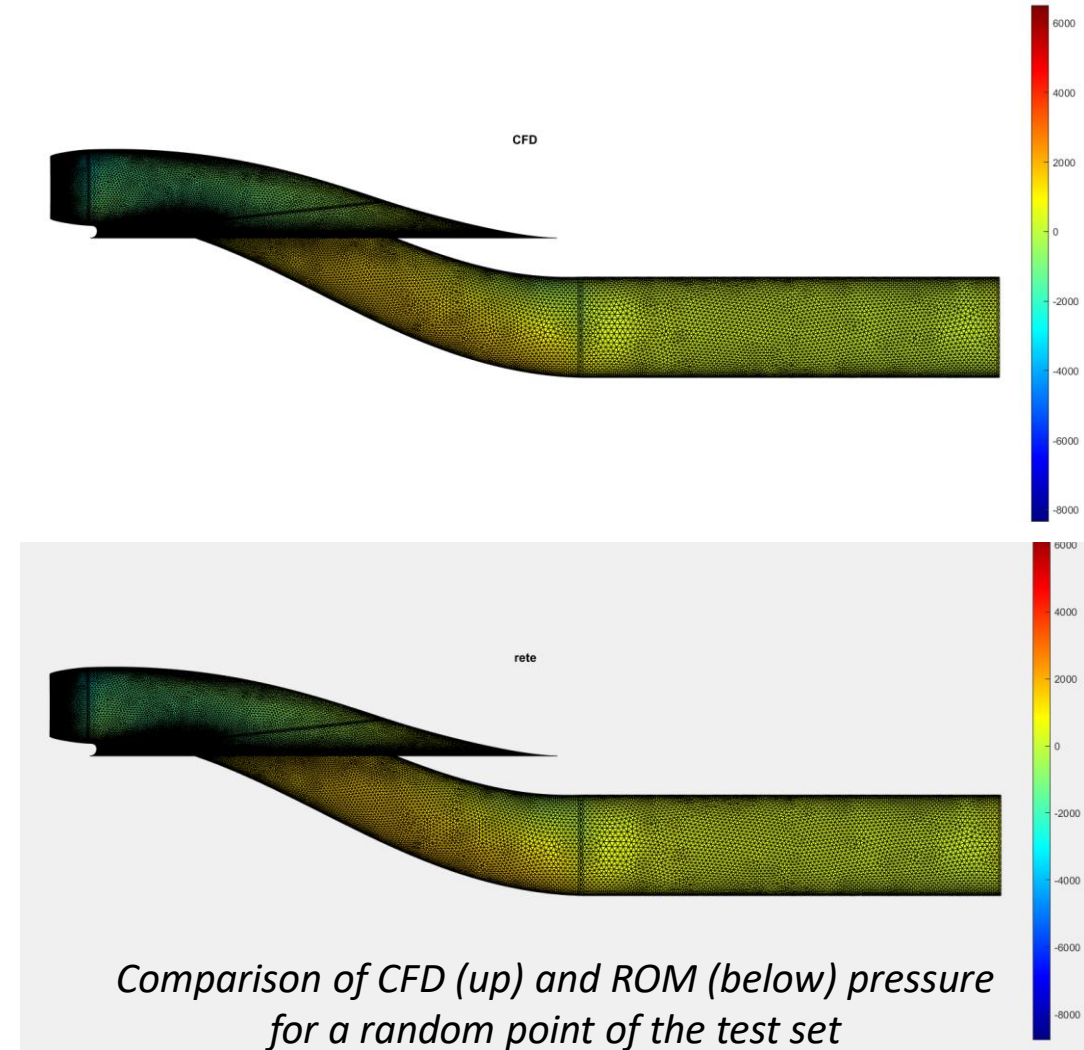
Input:

- 6 shape parameters
- Velocity
- Outlet massflow

Output:

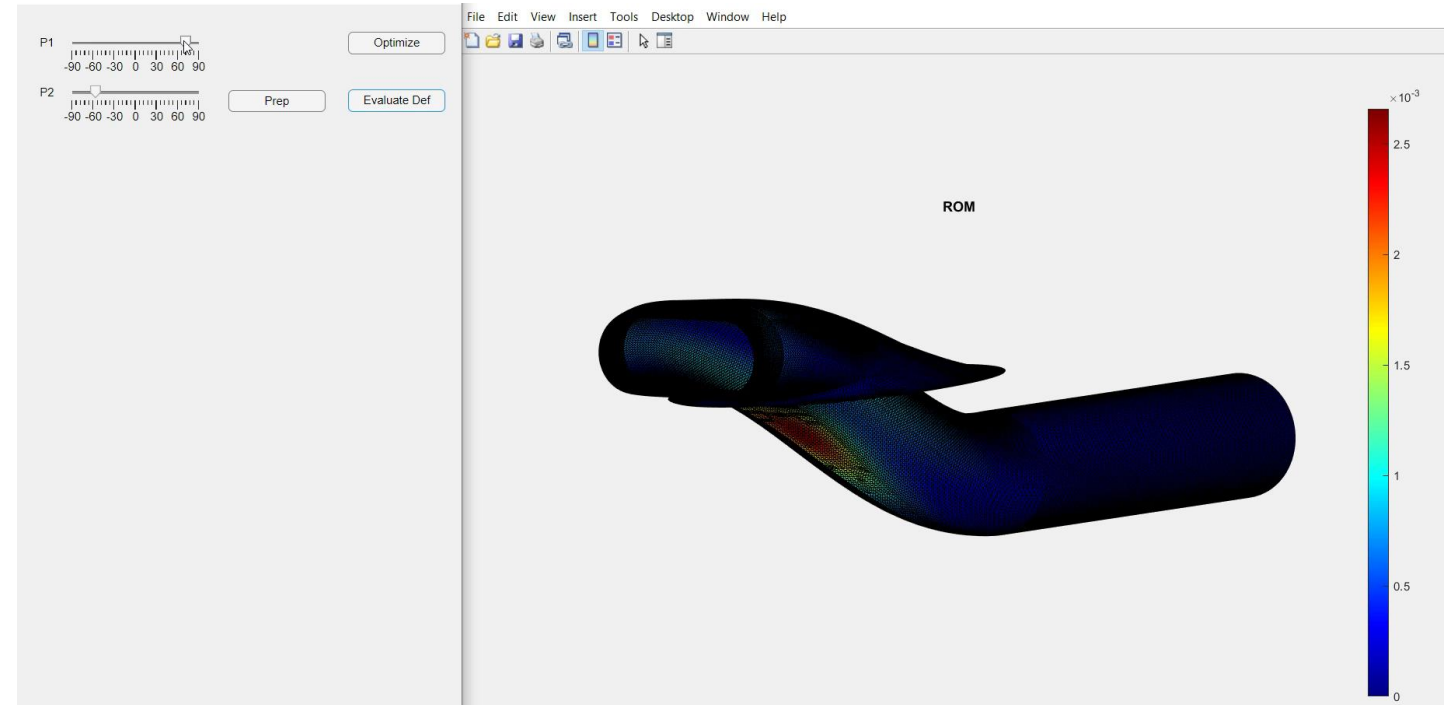
- Pressure field

ROM Relative error < 6%



Optimization dashboard

- Physical parameters are set and the optimum is identified;
- Field quantities can also be evaluated in real time;
- Accurate and reliable;
- Understanding of the physics of the problem.



FEM Optimization: Angle of plies

Baseline:

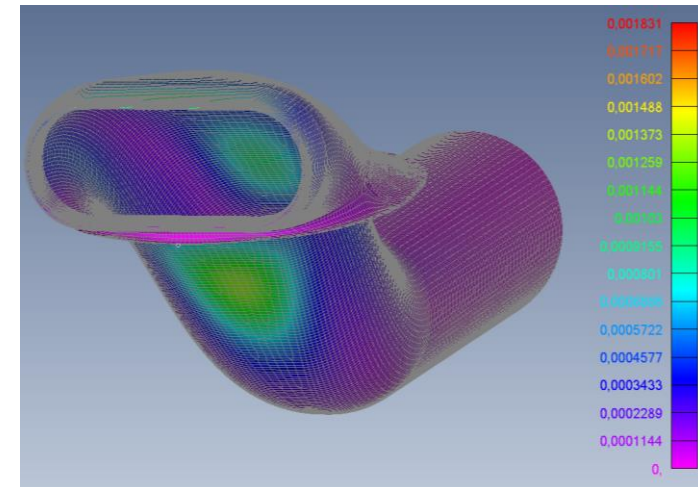
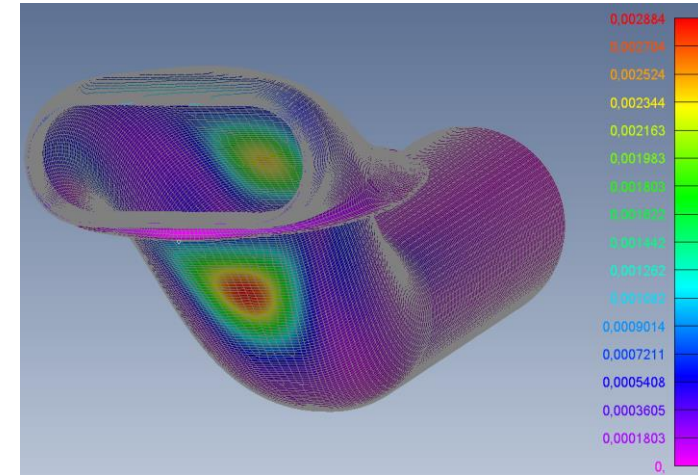
- Lamination sequence: $[0/90]_s$

Optimized angle:

- Lamination sequence: $[-90/0]_s$

Max Displacements reduction: -36%

| | Max Displacements [mm] |
|-----------|------------------------|
| Baseline | 2.88 |
| Optimized | 1.83 |



Displacements baseline (above) and optimized (below)

- CFD optimization: Drag -32% ; P_out +86%
- Mass reduction: Mass -92%
- FEM optimization: Max_displ -36%
- ROM development: ROM Realtive Error < 6%
- The workflow presented enables improved fluid dynamic and structural performance.
- The extracted ROMs allow real-time evaluation of the quantities of interest and can be used to create an optimization dashboard or can be integrated with visualization tool

Thank You For Your Attention

A. Lopez, U. Cella, C. Groth, M. E. Biancolini

Università di Roma, Tor Vergata